# The Crystal and Molecular Structure of Tetrameric Arsenic Selenide, As $\mathbf{A S e}_{4}$ 

By Paul Goldstein and Art Paton<br>Xerox Corporation, Xerox Square W-114, Rochester, New York 14644, U.S.A.

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#### Abstract

From an analysis of three-dimensional X-ray diffraction data, the crystal structure of $\mathrm{As}_{4} \mathrm{Se}_{4}$ has been shown to be isomorphous with that of realgar, the low-temperature form of $\mathrm{As}_{4} \mathrm{~S}_{4} . \mathrm{As}_{4} \mathrm{Se}_{4}$ crystallizes in space group $P 2_{1} / n$ with lattice constants $a=9 \cdot 552, b=13 \cdot 801, c=6 \cdot 719 \AA, \beta=106 \cdot 44^{\circ}, U=849 \cdot 5 \AA^{3}$, $Z=4$. Least-squares refinement based on 1466 unique reflections has led to a conventional $R$ of 0.054 . The cage-like $\mathrm{As}_{4} \mathrm{Se}_{4}$ molecule has approximate $\overline{4} 2 \mathrm{~m}$ symmetry with the following average bond distances and angles: As-Se $=2 \cdot 384 \pm 0.005, \mathrm{As}-\mathrm{As}=2 \cdot 566 \pm 0.008 \AA, \mathrm{As}-\mathrm{Se}-\mathrm{As}=98 \cdot 1 \pm 0 \cdot 3, \mathrm{Se}-\mathrm{As}-\mathrm{Se}=$ $94 \cdot 2 \pm 0 \cdot 3$, and $\mathrm{As}-\mathrm{As}-\mathrm{Se}=101 \cdot 2 \pm 0 \cdot 6^{\circ}$. The packing is dominated by short intermolecular separations of the type As $\cdots$ As and As $\cdots$ Se.


## Introduction

In their phase studies on the glass-forming As-Se system, Myers \& Felty (1967) isolated a crystalline compound at an $\mathrm{As} / \mathrm{Se}$ atomic ratio of 1. Preliminary crystallographic studies (Myers \& Felty, 1967) suggested that the structure of this compound, also reported by Dembovskii (1963), might be isomorphous with that of realgar, the naturally occurring form of $\mathrm{As}_{4} \mathrm{~S}_{4}$ (Ito, Morimoto \& Sadanaga, 1952), and hence should consist of $\mathrm{As}_{4} \mathrm{Se}_{4}$ molecules having the realgar structure. The structure determination of the material was undertaken to verify these deductions and to obtain accurate values for the As-Se bond length and the $\mathrm{Se}-\mathrm{As}-\mathrm{Se}$ and $\mathrm{As}-\mathrm{Se}-\mathrm{As}$ bond angles which could be used in the detailed interpretation of the radial distribution functions of vitreous As-Se alloys (Kaplow, Rowe \& Averbach, 1968). The only other source of these parameters was the limited structural study of $\mathrm{As}_{2} \mathrm{Se}_{3}$ by Vaipolin (1966).

## Experimental section

Black rod-shaped crystals of $\mathrm{As}_{4} \mathrm{Se}_{4}$ prepared by sublimation were obtained from J. Berkes of this laboratory. A crystal of dimensions $0.09 \times 0.10 \times 0.22 \mathrm{~mm}$ with its $c$ axis in the long direction was selected for study. From an analysis of precession photographs, the space group was verified to be $P 2_{1} / n$ and the lattice parameters were found to be similar to those of realgar. Accurate lattice parameters were derived by least-squares refinement of the $\varphi, \chi$ and $2 \theta$ settings of 44 carefully centered reflections on a Picker full-circle diffractometer. The values obtained are $a=9.552 \pm 0.002, \quad b=13.801 \pm$ $0.003, c=6.719 \pm 0.001 \AA, \beta=106.44 \pm 0.01^{\circ}$. Hence $U$, the volume of the unit cell is $849 \cdot 5 \pm 0 \cdot 3 \dot{\AA}^{3}$ and the calculated X-ray density $D_{x}$ is $4.811 \mathrm{~g} \mathrm{~cm}^{-3}$ for 4 molecules per unit cell.

## Data collection

The intensity data were collected in the $\theta-2 \theta$ scan mode on a Picker diffractometer controlled by a fourangle programmer and equipped with a modified IBM
card-reader card-punch. Mo $K \alpha$ radiation ( $\lambda=0.71069$ $\AA$ ) monochromated on the incident beam side by the 002 reflection from a graphite monochromator was utilized. The crystal of $\mathrm{As}_{4} \mathrm{Se}_{4}$ was oriented with its $c^{*}$ axis parallel to the $\varphi$ axis of the diffractometer and input settings calculated via DIFSET, F. P. Boer's modification of the Case Institute crystal orientation program (Knox, 1966). Scans were carried out at $1^{\circ}$ $\min ^{-1}$ over a $2 \theta$ range of $(\Delta+3)^{\circ}$ where $\Delta$ is the $2 \theta$ separation of the $\alpha_{1}$ and $\alpha_{2}$ components. Background counts were accumulated for 50 s at the ends of each scan range by the stationary-crystal stationary-counter method. Some 5000 reflections comprising a full sphere of data up to $50^{\circ}$ in $2 \theta$ were recorded. The 004 reflection was monitored after every 20 measurements to check that stability was maintained to $\pm 2 \%$ in the total intensity. Although the decomposition of realgar in the presence of light has been reported in the literature (Ito, Morimoto \& Sadanaga, 1952; Street \& Munir, 1970), this decomposition, if it occurred in $\mathrm{As}_{4} \mathrm{Se}_{4}$, would be localized on the surface of the crystal and hence should not have affected our results. The sharpness of the observed reflections and our ability to maintain the intensity of our standard reflection constant during data collection support this contention.

## Data processing and reduction

The net intensity $I_{\text {net }}$ and its error $\sigma_{I}$ were obtained from the scan count $P$ and the background counts $B_{1}$ and $B_{2}$ by the expressions: $I_{\text {net }}=P-t\left(B_{1}+B_{2}\right)$ and $\sigma_{I}=\left[P+t^{2}\left(B_{1}+B_{2}\right)+\left(0.03 I_{\text {net }}\right)^{2}\right]^{1 / 2}$, where $t$ is the ratio of the scan time to the total background time. The data were corrected for Lorentz and polarization factors by the expression (Lp) $)^{-1}=\sin 2 \theta(1+q) /\left(1+q \cos ^{2} 20\right)$, where $q=\cos ^{2} 2 \theta_{m}$ and $\theta_{m}$ is the Bragg angle at the graphite monochromator. An absorption correction based on a multi-faceted solid (Busing \& Levy, 1957) was applied ( $\mu=347 \mathrm{~cm}^{-1}$ ) via the routines $A B S R P 1$ and $A B S R P 2$ obtained from NRC (Ahmed \& Singh, 1967). The maximum and minimum values of the absorption correction on a relative scale were 1.571 and 0.691 , respectively. The maximum error in the correction is
estimated to be $12 \%$ on the basis of the differences between equivalent reflections after its application. Reduction of the data to a unique set of 1466 reflections was accomplished by averaging equivalent reflections according to the method of Hamilton, Rollett \& Sparks (1965) with a local version of Sparks's scaling program. The correlation procedure was carried out in two steps. Centrosymmetrically related reflections were averaged first, yielding a value of 0.036 for the discrepancy index

$$
G_{w}=\sum_{h k l}\left[\sum_{i}\left(I_{i}-\bar{I}_{h k l}\right)^{2}\right]^{1 / 2}\left(\sum_{i} w_{i}\right)^{1 / 2} / \sum_{h k l}\left(\sum_{i} w_{i}\right)^{1 / 2} I_{h k l}
$$

where $w_{i}=1 / \sigma^{2}\left(I_{i}\right)$ is the weight and $I_{i}$ is the intensity of one of a pair of averaged reflections, $\bar{I}_{h k l}$ is the resultant averaged intensity and the external sum is taken over all $h k l$ pairs. The remaining equivalent reflections were averaged following the application of the absorption correction. The value of $G_{w}$ for this step was 0.076 as opposed to a value of 0.098 had the absorption correction not been applied. The 37 unique reflections which had $I_{\text {net }} \leq \sigma_{I}$ were classified as unobserved.

## Structure determination and refinement

Precession photographs had indicated that the structure of $\mathrm{As}_{4} \mathrm{Se}_{4}$ was isomorphous with that of realgar (Ito, Morimoto \& Sadanaga, 1952). Refinement was therefore initiated by full-matrix least-squares techniques with starting values of the atomic fractional coordinates for As and Se taken from those of Ito et al. (1952) for As and S, respectively. A Wilson plot calculated as suggested by Rogers (1965) provided the initial values of the scale factor and the overall temperature factor. Atomic scattering factors for neutral As and Se atoms were obtained from Cromer \& Waber (1965) and dispersion corrections were applied to all atoms with Cromer's (1965) values of $\Delta f^{\prime}$ and $\Delta f^{\prime \prime}$. The function minimized was $\sum w\left(\left|F_{o}\right|-K\left|F_{c}\right|\right)^{2}$ where $w$, the weight associated with each observational equation, initially had the form

$$
\begin{gathered}
w=1 /(1 \cdot 9)^{2} \quad \text { for } \quad\left|F_{o}\right| \leq 4 F_{\min } \\
w=1 /\left(A+B\left|F_{o}\right|+C\left|F_{o}\right|^{2}\right) \text { for }\left|F_{o}\right| \geq 4 F_{\min }
\end{gathered}
$$

and
$F_{\min }$ was $2 \cdot 5, A, B$ and $C$ (Cruickshank, 1965) were given the values $1 \cdot 0,0 \cdot 20$ and $0 \cdot 005$, respectively, and the sum
was taken over all observed reflections as well as those unobserved reflections for which $\left|F_{o}\right|$ was smaller than $\left|F_{c}\right|$. Three cycles of least-squares refinement with isotropic temperature factors ( 33 parameters) reduced the conventional agreement index $R$ based on $F$ to 0.081 and the corresponding weighted agreement index $R_{w}$ to $0 \cdot 118$. Four additional cycles with anisotropic temperature factors on all atoms ( 73 parameters) yielded $R=0.063$ and $R_{w}=0.097$ for the 1432 reflections included in the refinement. The residual index $S=$ $\left(\sum w \Delta^{2} / m-n\right)^{1 / 2}$ was 0.60 . Three cycles of anisotropic refinement were then carried out (one would have been enough) with $w=1 / \sigma_{F}^{2}$ where $\sigma_{F}$ is the experimental error in $\left|F_{o}\right| . R$ and $R_{w}$ decreased to 0.052 and 0.037 , respectively, and $S$ became $2 \cdot 7$, but little change occurred in the parameters. The maximum shift during the last cycle was $0 \cdot 06 \sigma$ and the average shift was $0 \cdot 02 \sigma$. The final value of $R$ for all measured reflections is 0.054 . The calculations were carried out on an XDS SIGMA 7 computer. The least-squares program was GROUP 1, a version of ORFLS (Busing, Martin \& Levy, 1962) modified by Doedens (1970) for rigidgroup refinement.


Fig. 1. ORTEP drawing of the $\mathrm{As}_{4} \mathrm{Se}_{4}$ molecule along a direction perpendicular to both the $\operatorname{As}(1)-\operatorname{As}(4)$ and $\operatorname{As}(2)-\operatorname{As}(3)$ bonds. Contours for the thermal vibrational ellipsoids are shown at the $50 \%$ probability level. The distances of the atoms from the best least-squares plane through the four Se atoms are indicated.

Table 1. Final fractional coordinates and anisotropic thermal parameters
The standard deviations are given in parentheses. All values have been multiplied by $10^{5}$. The temperature factor is of the form

| $\exp \left[-\left(h^{2} \beta_{11}+k^{2} \beta_{22}+l^{2} \beta_{33}+2 h k \beta_{12}+2 h l \beta_{13}+2 k l \beta_{23}\right)\right]$. |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $x / a$ | $y / b$ | $z / c$ | $\beta_{11}$ | $\beta_{22}$ | $\beta_{33}$ | $\beta_{12}$ | $\beta_{13}$ | $\beta_{23}$ |
| As(1) | 11545 (11) | 1809 (7) | -24346 (16) | 601 (13) | 240 (6) | 1172 (27) | 64 (7) | 187 (15) | 70 (10) |
| As(2) | 42758 (11) | -14054 (7) | -13653 (17) | 461 (12) | 253 (6) | 1408 (28) | 11 (6) | 322 (15) | -42 (10) |
| As(3) | 32513 (11) | - 13104 (8) | 17546 (16) | 509 (12) | 302 (6) | 1009 (26) | 11 (7) | 157 (14) | 65 (10) |
| As(4) | 3746 (11) | -16022 (8) | - 29701 (17) | 488 (12) | 296 (6) | 1264 (27) | -64 (7) | 119 (15) | -69 (10) |
| $\mathrm{Se}(1)$ | 34925 (11) | 958 (7) | -30587 (16) | 676 (13) | 257 (6) | 1277 (27) | -62 (7) | 408 (15) | 36 (9) |
| $\mathrm{Se}(2)$ | 21289 (11) | 2465 (7) | 12330 (16) | 583 (13) | 278 (6) | 1226 (26) | 18 (7) | 276 (15) | -102 (10) |
| Se (3) | 24200 (12) | -23215 (7) | -37278 (17) | 738 (14) | 256 (6) | 1423 (28) | -45 (7) | 364 (16) | -150 (10) |
| $\mathrm{Se}(4)$ | 10211 (12) | -21803 (8) | 4990 (17) | 654 (14) | 330 (6) | 1469 (29) | -106 (7) | 393 (16) | 102 (10) |

## Results and discussion

Values of the positional coordinates and anisotropic thermal parameters at the end of the least-squares refinement are given in Table 1. Intramolecular distances and angles associated with bonded and non-bonded atoms are presented in Table 2. The e.s.d.'s derived from the inverse least-squares matrix range from 0.0013 to $0.0018 \AA$ in the distances and from 0.03 to $0.06^{\circ}$ in the angles. The errors in the librational correction increase these e.s.d.'s by approximately $0.001 \AA$ and $0.05^{\circ}$, respectively. $\dagger$

Table 2. Intramolecular distances ( $\AA$ ) and angles $\left({ }^{\circ}\right)$ in $\mathrm{As}_{4} \mathrm{Se}_{4}$
The average estimated standard deviations are $0.003 \AA$ in the distances and $0 \cdot 1^{\circ}$ in the angles.
Values in parentheses are before correction for librational motion.

| As(1)---As(4) | $2 \cdot 571$ (2.567) | $\mathrm{As}(1)-\mathrm{Se}(1)-\mathrm{As}(2)$ | 崖 |
| :---: | :---: | :---: | :---: |
| $\mathrm{As}(2)-\mathrm{As}(3)$ | $2 \cdot 560$ (2.556) | $\mathrm{As}(2)-\mathrm{Se}(3)-\mathrm{As}(4)$ | 97.9 |
| $\mathrm{As}(1)-\mathrm{Se}(1)$ | 2.393 (2.389) | As(4)--Se(4)--As(3) | $97 \cdot 8$ |
| $\mathrm{As}(2)-\mathrm{Se}(1)$ | $2 \cdot 385$ (2.380) | $\mathrm{As}(3)-\mathrm{Se}(2)-\mathrm{As}(1)$ | 98.4 |
| $\mathrm{As}(2)-\mathrm{Se}$ (3) | 2.384 (2.381) | $\mathrm{Se}(1)-\mathrm{As}(2)-\mathrm{Se}(3)$ | $94 \cdot 0$ |
| $\mathrm{As}(4)-\mathrm{Se}(3)$ | 2.376 (2.372) | $\mathrm{Se}(3)-\mathrm{As}(4)-\mathrm{Se}(4)$ | 93 |
| $\mathrm{As}(4)-\mathrm{Se}(4)$ | 2.378 (2.374) | $\mathrm{Se}(4)-\mathrm{As}(3)-\mathrm{Se}(2)$ | 94.7 |
| $\mathrm{As}(3)-\mathrm{Se}(4)$ | 2.386 (2.382) | $\mathrm{Se}(2)-\mathrm{As}(1)-\mathrm{Se}(1)$ | $94 \cdot 2$ |
| $\mathrm{As}(3)-\mathrm{Se}(2)$ | 2.387 (2.383) | $\mathrm{As}(4)-\mathrm{As}(1)-\mathrm{Se}(2)$ | $101 \cdot 2$ |
| $\mathrm{As}(1)-\mathrm{Se}(2)$ | 2.381 (2.377) | $\mathrm{As}(4)-\mathrm{As}(1)-\mathrm{Se}(1)$ | $100 \cdot 2$ |
| $\mathrm{Se}(1) \cdots \mathrm{Se}(3)$ | 3.487 (3.481) | $\mathrm{As}(3)-\mathrm{As}(2)-\mathrm{Se}(1)$ | $101 \cdot 9$ |
| $\mathrm{Se}(3) \cdots \mathrm{Se}$ (4) | 3.475 (3.470) | $\mathrm{As}(3)-\mathrm{As}(2)-\mathrm{Se}(3)$ | $100 \cdot$ |
| $\mathrm{Se}(4) \cdots \mathrm{Se}(2)$ | $3 \cdot 511$ (3.505) | $\mathrm{As}(1)-\mathrm{As}(4)-\mathrm{Se}(3)$ | $102 \cdot 0$ |
| $\mathrm{Se}(2) \cdots \mathrm{Se}$ (1) | $3.496(3.490)$ | $\mathrm{As}(1)-\mathrm{As}(4)-\mathrm{Se}(4)$ | $101 \cdot 6$ |
| $\mathrm{As}(1) \cdots \mathrm{As}(2)$ | 3.610 (3.603) | $\mathrm{As}(2)-\mathrm{As}(3)-\mathrm{Se}(4)$ | $101 \cdot 3$ |
| As(2) $\cdots$ As(4) | $3 \cdot 591(3 \cdot 584)$ | $\mathrm{As}(2)-\mathrm{As}(3)-\mathrm{Se}(2)$ | $100 \cdot 7$ |
| As(4) $\cdots$ As $(3)$ | $3 \cdot 591$ (3.585) | $\mathrm{Se}(1) \cdots \mathrm{Se}(3) \cdots \mathrm{Se}(4)$ | $90 \cdot 5$ |
| $\operatorname{As}(3) \cdots \operatorname{As}(1)$ | $3 \cdot 610$ (3.603) | $\mathrm{Se}(3) \cdots \mathrm{Se}(4) \cdots \mathrm{Se}(2)$ | 89.9 |
|  |  | $\mathrm{Se}(4) \cdots \mathrm{Se}(2) \cdots \mathrm{Se}(1)$ | $89 \cdot 7$ |
|  |  | $\mathrm{Se}(2) \cdots \mathrm{Se}(1) \cdots \mathrm{Se}(3)$ | $89 \cdot 9$ |

## Molecular geometry

The crystal structure of $\mathrm{As}_{4} \mathrm{Se}_{4}$ is isomorphous with that of realgar (Ito, Morimoto\& Sadanaga, 1952). The $\mathrm{As}_{4} \mathrm{Se}_{4}$ molecule, like that of realgar $\left(\mathrm{As}_{4} \mathrm{~S}_{4}\right)$, has a cage-like structure (Fig. 1) in which a square of Se atoms bisects a distorted tetrahedron of As atoms. The distances of the As and Se atoms from the best least-

[^0]squares plane through the four Se atoms are shown in Fig. 1. The equation of this plane is $0.7474 X+0.2841 Y$ $-0 \cdot 6006 Z+1 \cdot 716=0$, where $X, Y, Z$ are orthogonal coordinates in $\AA$ along the crystallographic axes $a, b$ and $c^{*}$, respectively. Table 3 presents some of the torsion angles. The deviations from ideal $\overline{4} 2 m$ symmetry are small but significant and presumably stem from the non-uniform crystallographic environment of the $\mathrm{As}_{4} \mathrm{Se}_{4}$ molecules.

## Bond distances and angles

The average values of the intramolecular distances and angles in the structures of $\mathrm{As}_{4} \mathrm{Se}_{4}$ and $\mathrm{As}_{4} \mathrm{~S}_{4}$ are compared in Table 4. The average As-As bond length in $\mathrm{As}_{4} \mathrm{Se}_{4}, 2 \cdot 566 \AA$, is intermediate between $2 \cdot 59 \AA$, the value reported by Ito et al. (1952) in realgar, and $2 \cdot 49$ $\AA$, the value reported by Lu \& Donohue (1944) in gaseous $\mathrm{As}_{4} \mathrm{~S}_{4}$. These values are considerably longer than $2.42 \AA$, the covalent diameter of the As atom (Schomaker \& Stevenson, 1941). By comparison, the As-As bond length is $2 \cdot 44 \AA$ in gaseous $\mathrm{As}_{4}$ (Maxwell, Hendricks \& Moseley, 1935), $2 \cdot 477 \pm 0.003 \AA$ in $\mathrm{As}_{4} \mathrm{~S}_{3}$ (Whitfield, 1970), $2 \cdot 428 \pm 0 \cdot 008 \AA$ in (MeAs) ${ }_{3}$ (Burns \& Waser, 1957) and $2 \cdot 456 \pm 0.005 \AA$ in (PhAs) ${ }_{6}$ (Hedberg, Hughes \& Waser, 1961). In rhombohedral As, where the distance between an As atom and its three nearest neighbors is $2.517 \AA$ (Schiferl \& Barrett, 1969), each As atom also has three other neighbors $3.12 \AA$, away and the lengthening of the As-As bond can be ascribed to partial metallic bonding (Mooser \& Pearson, 1958). In $\mathrm{As}_{4} \mathrm{Se}_{4}$ and $\mathrm{As}_{4} \mathrm{~S}_{4}$, however, the elongation of the As-As bond must arise from the preference of the molecules for a bonding configuration having $\overline{4} 2 m$ symmetry concomitant with a minimization of the intramolecular repulsions between non-bonded atoms. Evidence of these repulsions is seen in the short average intramolecular $\mathrm{Se} \cdots$ Se separations $(3 \cdot 49 \pm$ $0.01 \AA$ ) in $\mathrm{As}_{4} \mathrm{Se}_{4}$. By contrast, the shortest intra-ring and intra-chain non-bonded $\mathrm{Se} \cdots \mathrm{Se}$ separations are, respectively, $3.72 \pm 0.04 \AA$ in $\alpha$-Se (Cherin \& Unger, 1972) and $3.716 \AA$ in trigonal Se (Cherin \& Unger, 1967).

The importance of atomic contact diameters in stabilizing the geometry of the $\mathrm{As}_{4} \mathrm{X}_{4}$ molecule is brought out further if one compares the average values of the shortest non-bonded intramolecular separations between atoms at the tetrahedral positions (As) to those between atoms at the square positions ( S or Se ). One finds that the differences have the same sign and

Table 3. Values of the smaller torsion angles in the $\mathrm{As}_{4} \mathrm{Se}_{4}$ molecule
The torsion angle $A-B-C-D$ is defined as the dihedral angle between planes $A B C$ and $B C D$. It is taken as positive if the projection of bond $C D$ onto the plane perpendicular to bond $B C$ lies clockwise to the projection of bond $B A$ when seen along bond $B C$.

| 1)- $\mathrm{As}(2)-\mathrm{As}(3)-\mathrm{Se}(2)$ | $-1.2$ |
| :---: | :---: |
| $\mathrm{Se}(3)-\mathrm{As}(2)-\mathrm{As}(3)-\mathrm{Se}(4)$ | -0.5 |
| $\mathrm{Se}(1)-\mathrm{As}(1)-\mathrm{As}(4)-\mathrm{Se}(3)$ | 0.8 |
| $\mathrm{Se}(2)-\mathrm{As}(1)-\mathrm{As}(4)-\mathrm{Se}(4)$ | 1.0 |
| $\mathrm{As}(4)-\mathrm{As}(1)-\mathrm{Se}(1)-\mathrm{As}(2)$ | 39 |
| $\mathrm{As}(3)-\mathrm{As}(2)-\mathrm{Se}(1)-\mathrm{As}(1)$ | 37 |


| $\operatorname{As}(3)-\operatorname{As}(2)-\mathrm{Se}(3)-\mathrm{As}(4)$ | $39 \cdot 2^{\circ}$ |
| :--- | ---: |
| $\operatorname{As}(1)-\operatorname{As}(4)-\mathrm{Se}(3)-\operatorname{As}(2)$ | $38 \cdot 1$ |
| $\operatorname{As}(1)-\operatorname{As}(4)-\mathrm{Se}(4)-\operatorname{As}(3)$ | $-38 \cdot 9$ |
| $\operatorname{As}(2)-\operatorname{As}(3)-\operatorname{Se}(4)-\operatorname{As}(4)$ | $-38 \cdot 4$ |
| $\operatorname{As}(2)-\operatorname{As}(3)-\operatorname{Se}(2)-\operatorname{As}(1)$ | $39 \cdot 4$ |
| $\operatorname{As}(4)-\operatorname{As}(1)-\operatorname{Se}(2)-\operatorname{As}(3)$ | $37 \cdot 3$ |

possess magnitudes which range from $0 \cdot 11 \AA$ in $\mathrm{As}_{4} \mathrm{Se}_{4}$ to $0.18 \AA$ in $\mathrm{As}_{4} \mathrm{~S}_{4}$. The same relationship between the non-bonded separations of atoms at the two different sites occurs in the molecules of $\mathrm{N}_{4} \mathrm{~S}_{4}$ (Sharma \& Donohue, 1963) and $\mathrm{N}_{4} \mathrm{Se}_{4}$ (Bärnighausen, von Volkmann \& Jander, 1966), which also crystallize with approximate $\overline{4} 2 m$ symmetry except that now the N atoms lie at the corners of a square and the S or Se atoms occupy the distorted tetrahedral positions. The average values in the intramolecular non-bonded separations of the type $\mathrm{N} \cdots \mathrm{N}$ and $\mathrm{X} \cdots \mathrm{X}$, where $\mathrm{X}=\mathrm{S}$ or Se, are 2.55 and $2.69 \AA$ respectively in $\mathrm{N}_{4} \mathrm{~S}_{4}$, and 2.78 and $2.97 \AA$ in $\mathrm{N}_{4} \mathrm{Se}_{4}$. The atoms at the tetrahedral positions ( S or Se ) are therefore again further from one another than the atoms at the square positions ( N ) this time by $0.14 \AA$ in $\mathrm{N}_{4} \mathrm{~S}_{4}$ and $0.19 \AA$ in $\mathrm{N}_{4} \mathrm{Se}_{4}$.

Table 4. Average values of the intramolecular distances and angles in $\mathrm{As}_{4} \mathrm{X}_{4}(\mathrm{X}=\mathrm{Se}, \mathrm{S})$ and the root mean square deviations in these values
The values for $\mathrm{As}_{4} \mathrm{~S}_{4}$ were obtained directly from the atomic coordinates published by Ito, Morimoto \& Sadanaga (1952) with the use of their reported lattice parameters. The starred values $\left({ }^{*}\right)$ differ both from the average values quoted by these authors in their paper and from the values derived from their Table 4.

|  | $\mathrm{X}=\mathrm{Se}$ | $\mathrm{X}=\mathrm{S}$ |
| :---: | :---: | :---: |
| As-X | $2.384 \pm 0.005 \AA$ | $2.24 \pm 0.04 \AA$ |
| As--As | $2.566 \pm 0.008$ | $2.595 \pm 0.007^{*}$ |
| As-X-As | $98.1 \pm 0.3^{\circ}$ | $101 \cdot 8 \pm 0 \cdot 7^{\circ}$ * |
| X-As-X | $94 \cdot 2 \pm 0 \cdot 3$ | $94 \cdot 6 \pm 3 \cdot 5^{*}$ |
| As-As-X | $101 \cdot 2 \pm 0 \cdot 6$ | $99.0 \pm 1 \cdot 3^{*}$ |
| X $\cdot \cdots$ X | $3.492 \pm 0.015$ | $3.30 \pm 0.04$ * |
| As..As | $3.601 \pm 0.011$ | $3.48 \pm 0.04$ |
| As $\cdot$. X | $3.827 \pm 0.014$ | $3.68 \pm 0.05$ |
| X $\cdots$. ${ }^{\text {P }}$. X | $90 \cdot 0 \pm 0 \cdot 3^{\circ}$ | $90.0 \pm 1 \cdot 2^{\circ}$ |

The average As-Se bond length found in $\mathrm{As}_{4} \mathrm{Se}_{4}$, $2 \cdot 384 \pm 0.005 \AA$, is equal to the sum of the covalent radii of As and Se and slightly shorter than the average As-Se bond length ( $2.41 \pm 0.05 \AA$ ) reported in crystalline $\mathrm{As}_{2} \mathrm{Se}_{3}$ (Vaipolin, 1966). No other accurate crystal structures containing As-Se bond lengths are available for comparison. However, the As-Se bond length in $\mathrm{As}_{4} \mathrm{Se}_{4}$ is consistent with the As-S bond length in realgar, $2 \cdot 24 \pm 0.04 \AA$, if the effect of substituting Se
for S is taken to correspond to the difference between 1.17 and $1.04 \AA$, the covalent radii of Se and S, respectively (Schomaker \& Stevenson, 1941). A comparison of the average bond angles in $\mathrm{As}_{4} \mathrm{Se}_{4}$ and $\mathrm{As}_{4} \mathrm{~S}_{4}$ (Table 4) shows that corresponding $X$-As- $X$ angles ( $X=S, S e$ ) are the same but corresponding As-As-X and As-XAs angles differ somewhat. The observed difference in the As-X-As angles is consistent with the effect on the $\mathrm{Y}-\mathrm{X}-\mathrm{Y}$ angle of substituting $\mathrm{X}=\mathrm{Se}$ for $\mathrm{X}=\mathrm{S}$. This effect is illustrated in Table 5 by examples taken from the literature. The average value of the bond angle at the Se atom reported by Vaipolin (1966) in $\mathrm{As}_{2} \mathrm{Se}_{3}$ seems to be rather low according to this analysis. However, a recent refinement of the structure of $\mathrm{As}_{2} \mathrm{Se}_{3}$ by least-squares methods using Vaipolin's observed structure factors (Goldstein, 1973) has yielded structural parameters more in line with those of $\mathrm{As}_{2} \mathrm{~S}_{3}$ (Morimoto, 1954), namely $2 \cdot 40 \pm 0.04 \AA$ for the average As-Se bond length and $95.4 \pm 8.0$ and $98.9 \pm 6 \cdot 4^{\circ}$ for the average As-Se-As and $\mathrm{Se}-\mathrm{As}-\mathrm{Se}$ bond angles, respectively.

## Thermal motion

The analysis of rigid-body motion by the method of Schomaker \& Trueblood (1968) gave extremely good agreement between the observed and calculated thermal parameters, as indicated by the value of $0.027 \AA^{2}$ for the agreement factor $\left(\Sigma \Delta^{2} / \Sigma U_{i j}\right)^{1 / 2}$ and $0.0005 \AA^{2}$ for the r.m.s. $\Delta U_{i j}$. The fit to the thermal parameters in the present case is considerably better than that obtained by Forder (1971) in his analysis of rigid-body motion in phosphorus chalcogenides having cage-like structures and seems to preclude the presence of gross systematic errors associated with improper absorption corrections. The principal values, namely $2 \cdot 80,2 \cdot 64$ and $2.33^{\circ}$ for the librational tensor and $0.143,0.131$ and $0.141 \AA$ for the translational tensor, are similar to, albeit more nearly isotropic than, those reported by Forder. The librational correction consequently increases the bond distances by 0.003 to $0.005 \AA$ without altering the bond angles. The orientations and shapes of the individual vibrational ellipsoids are shown in Fig. 1, which was drawn with the ORTEP program (Johnson, 1965).

Table 5. Mean values and root mean square deviations from the mean of the bond angles at the S and Se atoms in a number of pairs of homologous compounds containing these elements

|  | $\mathrm{X}=\mathrm{S}$ | $\mathrm{X}=\mathrm{Se}$ | Compound | Reference |
| :--- | :---: | :---: | :---: | :---: |
| As-X-As | $101 \cdot 8 \pm 0 \cdot 7^{\circ}$ | $98 \cdot 1 \pm 0 \cdot 3^{\circ}$ | $\mathrm{As}_{4} \mathrm{X}_{4}$ | $(a)$ |
| $\mathrm{N}-\mathrm{X}-\mathrm{N}$ | $104 \cdot 5 \pm 0 \cdot 8$ | $10 \cdot 2 \pm \pm 0 \cdot 1$ | $\mathrm{~N}_{4} \mathrm{X}_{4}$ | $(b)$ |
| $\mathrm{P}-\mathrm{X}-\mathrm{P}$ | $103 \cdot 0 \pm 0 \cdot 4$ | $100 \cdot 1 \pm 0 \cdot 6$ | $\mathrm{P}_{4} \mathrm{X}_{3}$ | $(c)$ |
| $\mathrm{C}-\mathrm{X}-\mathrm{C}$ | $91 \cdot 5$ | $86 \cdot 7$ | $\mathrm{C}_{10} \mathrm{H}_{8} \mathrm{X}$ | $(d)$ |
| $\mathrm{X}-\mathrm{X}-\mathrm{X}$ | $107 \cdot 9 \pm 0 \cdot 6$ | $105 \cdot 6 \pm 1 \cdot 8$ | $\mathrm{X}_{8}$ | $(e)$ |
| $\mathrm{As}-\mathrm{X}-\mathrm{As}$ | $99 \pm 4$ | $89 \pm 3$ | $\mathrm{As}_{2} \mathrm{X}_{3}$ | $(f)$ |

(a) $\mathrm{As}_{4} \mathrm{~S}_{4}$ (from Table 4); $\mathrm{As}_{4} \mathrm{Se}_{4}$ (present work).
(b) $\mathrm{N}_{4} \mathrm{~S}_{4}$ (Sharma \& Donohue, 1963); $\mathrm{N}_{4} \mathrm{Se}_{4}$ (Bärnighausen et al., 1966).
(c) $\mathrm{P}_{4} \mathrm{~S}_{3}$ (Leung et al., 1957); $\mathrm{P}_{4} \mathrm{Se}_{3}$ (Keulen \& Vos, 1959).
(d) Dibenzothiophene, $\mathrm{C}_{10} \mathrm{H}_{8} \mathrm{~S}$ (Schaffrin \& Trotter, 1970); dibenzoselenophene, $\mathrm{C}_{10} \mathrm{H}_{8} \mathrm{Se}$ (Hope, Knobler \& McCullough, 1970) .
(e) Orthorhombic S (Abrahams, 1955; Caron \& Donohue, 1961); monoclinic $\alpha$-Se (Cherin \& Unger, 1970).
(f) $\mathrm{As}_{2} \mathrm{~S}_{3}$ (Morimoto, 1954); $\mathrm{As}_{2} \mathrm{Se}_{3}$ (Vaipolin, 1966).


Fig. 2. View of the crystal structure of $\mathrm{As}_{4} \mathrm{Se}_{4}$ along the $a$ axis. The designations are $A, B, C$ and $D$ for molecules at $x, y$, $z$; $-x,-y,-z ; \frac{1}{2}+x, \frac{1}{2}-y, \frac{1}{2}+z ; \frac{1}{2}-x, \frac{1}{2}+y, \frac{1}{2}-z$, respectively. The subscripts specify the lattice translations to be applied to these molecules.


## Molecular packing

The packing arrangement is the same as the one found in realgar (Ito et al., 1952). The intermolecular distances less than $3.70 \AA$ are shown in Figs. 2 and 3 which present $O R T E P$-derived views of the structure projected along directions parallel to the $a$ and $c$ axes, respectively. A close correspondence exists between these intermolecular separations, which are considerably shorter than the predicted van der Waals distance of $4 \cdot 0 \AA$ (Pauling, 1960), and those occurring in realgar. Analogously short intermolecular separations have also been reported in the structure of $\alpha-\mathrm{Se}$ (Cherin \& Unger, 1972), where they have been taken to imply the presence of relatively strong intermolecular interactions. However, they also suggest that Pauling's values for the van der Waals radii of the As and Se atoms may be too large. More appropriate values based on the intramolecular separations in $\alpha$-Se and arsenobenzene (Hedberg, Hughes \& Waser, 1961) would be $1.85 \AA$ for Se and $1.8 \AA$ for As. With these values for the contact radii, only separations of the type As $\cdots \mathrm{Se}$ and As...As would be shorter than the van der Waals contact distances in crystalline $\mathrm{As}_{4} \mathrm{Se}_{4}$ and hence could be associated with strong intermolecular interactions. A similar situation exists in realgar where all the intermolecular distances less than $3.72 \AA$ are either of the type As...S or As...As.

## References

Abrahams, S. C. (1955). Acta Cryst. 8, 661-671.
Ahmed, F. R. \& Singh, P. (1967). NRC Crystallographic Programs for the IBM $/ 360$ System, Program NRC-3. National Research Council, Ottawa, Canada.
bärnighausen, h., von Volkmann, T. \& Jander, J. (1966). Acta Cryst. 21, 571-577.

Burns, J. H. \& Waser, J. (1957). J. Amer. Chem. Soc. 79, 859-864.
Busing, W. R. \& Levy, H. A. (1957). Acta Cryst. 10, 180-182.
Busing, W. R., Martin, K. O. \& Levy, H. A. (1962). ORFLS. Report ORNL-TM-305, Oak Ridge National Laboratory, Oak Ridge, Tennessee.
Caron, A. \& Donohue, J. (1961). Acta Cryst. 14, 548-549.
Cherin, P. \& Unger, P. (1967). Inorg. Chem. 6, 1589-1591.
Cherin, P. \& Unger, P. (1972). Acta Cryst. B28, 313-317.
Cromer, D. T. (1965). Acta Cryst. 18, 17-23.
Cromer, D. T. \& Waber, J. T. (1965). Acta Cryst. 18, 104 109.

Cruickshank, D. W. J. (1965). In Computing Methods in Crystallography. Edited by J. S. Rollett, chap. 14. New York: Pergamon Press.

Dembovski, S. A. (1963). Zh. Neorgan. Khim. 8, 1534-1535.
Doedens, R. J. (1970). In Crystallographic Computing. Edited by F. R. Ahmed, pp. 198-200. Copenhagen: Munksgaard.
Forder, R. A. (1971). Acta Cryst. A27, 383-387.
Goldstein, P. (1973). In preparation.
Hamilton, W. C., Rollett, J. S. \& Sparks, R. A. (1965). Acta Cryst. 18, 129-130.
Hedberg, K., Hughes, E. W. \& Waser, J. (1961). Acta Cryst. 14, 369-374.
Hope, H., Knobler, C. \& McCullough, J. D. (1970). Acta Cryst. B26, 628-640.
Ito, T., Morimoto, N. \& Sadanaga, R. (1952). Acta Cryst. 5, 775-782.
Johnson, C. K. (1965). ORTEP. Report ORNL-3794, Oak Ridge National Laboratory, Oak Ridge, Tennessee.
Kaplow, R., Rowe, T. A. \& Averbach, B. L. (1968). Phys. Rev. 168, 1068-1079.
Keulen, E. \& Vos, A. (1959). Acta Cryst. 12, 323-329.
Knox, K. (1966). Program for Determining the Orientation of a Crystal in the Picker Goniostat by a Least-Squares Technique and for Generating the Necessary Cards to Scan any Set of Reflections by the $2 \theta$ Technique. Case Institute, Cleveland, Ohio.
leung, Y. C., Waser, J., van houten, S., Vos, A., Wiegers, G. A. \& Wiebenga, E. H. (1957). Acta Cryst. 10, 574-582.
Lu, C. S. \& Donohue, J. (1944). J. Amer. Chem. Soc. 66, 818-827.
Maxwell, L. R., Hendricks, S. B. \& Moseley, V. M. (1935). J. Chem. Phys. 3, 699-709.

Mooser, E. \& Pearson, W. B. (1958). J. Phys. Chem. Solids, 7, 65-77.
Morimoto, N. (1954). Miner. J. 1, 160-169.
Myers, M. B. \& Felty, E. J. (1967). Mater. Res. Bull. 2, 535-546.
Pauling, L. (1960). The Nature of the Chemical Bond, 3rd ed., p. 282. Ithaca: Cornell Univ. Press.
Rogers, D. (1965). In Computing Methods in Crystallography. Edited by J. S. Rollett, chap. 16. New York: Pergamon Press.
Schaffrin, R. M. \& Trotter, J. (1970). J. Chem. Soc. (A), pp. 1561-1565.
Schiferl, D. \& barrett, C. S. (1969). J. Appl. Cryst. 2, 30-36.
Schomaker, V. \& Stevenson, D. P. (1941). J. Amer. Chem. Soc. 63, 37-40.
Schomaker, V. \& Trueblood, K. N. (1968). Acta Cryst. B24, 63-76.
Sharma, B. D. \& Donohue, J. (1963). Acta Cryst. 16, 891-897.
Street, G. B. \& Munir, Z. A. (1970). J. Inorg. Nucl. Chem. 32, 3769-3774.
Vaipolin, A. A. (1966). Sov. Phys. Crystallogr. 10, 509-512.
Whitrield, H. J. (1970). J. Chem. Soc. (A), pp. 1800-1803.


[^0]:    $\dagger$ A list of observed and calculated structure factors has been deposited with the British Library Lending Division as Supplementary Publication No. SUP 30308 ( 27 pp., 1 microfiche). Copies may be obtained through the Executive Secretary, International Union of Crystallography, 13 White Friars, Chester CH1 1 NZ, England.

